



**Version (A) – MODEL ANSWER**

**Answer the following THREE questions:**

**(Total Marks: 15)**

**Question 1:**

**marks: 5**

- a) (3 marks) Dieticians إحصائي التغذية are concerned about sugar consumption in teenagers' diets (a 12-ounce can of soft drink typically has 10 teaspoons of sugar). In a random sample of 55 students, the number of teaspoons of sugar consumed for each student on a randomly selected day is tabulated. Summary statistics are noted as: **Min = 10, Max = 60, First quartile = 25, Third quartile = 38, Median = 31, Mean = 31.4, n = 55, and S = 11.6,**
- Find the interquartile range.  

$$\text{IQR} = \text{Q3} - \text{Q1} = 38 - 25 = 13$$
  - What is the shape of distribution?  
**Positive or (Right) Skewing**
  - What could you conclude about the value of 60?  

$$\text{Q1}-1.5(\text{IQR}) = 25 - 1.5(13) = 5.5$$

$$\text{Q3}+1.5(\text{IQR}) = 38 + 1.5(13) = 57.5$$
**Sinc 60 > 57.5 → 60 is an outlier.**
- b) (2 marks) Suppose the average score on a national test is 500 with a standard deviation of 100. If each score is increased by 25, what are the new mean and standard deviation?  

$$\mu_1 = 500, \sigma_1 = 100$$
**After increasing the score by 25 →  $\mu_2 = 525, \sigma_2 = \sigma_1 = 500$**

**Question 2:**

**marks: 5**

A recent study noted prices in US Dollars and battery lives in hours of 10 top-selling tablet computers. The data follow:

	1	2	3	4	5	6	7	8	9	10
Cost (X)	303	450	260	480	540	390	350	400	600	450
Battery Life (Y)	8.5	10	7	11	10	9	8	9.5	11	9.5

- a) (3 mark) Calculate the correlation coefficient between the cost of tablets and their battery lives and **Comment** on its value. ( $\bar{x} = 422.3, \bar{y} = 9.35, S_x = 104.1559, S_y = 1.2704$ ).

X	303	450	260	480	540	390	350	400	600	450	
Zx	-1.1454	0.26595	-1.5582	0.55398	1.13004	-0.3101	-0.6942	-0.2141	1.7061	0.26595	
Y	8.5	10	7	11	10	9	8	9.5	11	9.5	
Zy	-0.6691	0.51165	-1.8498	1.2988	0.51165	-0.2755	-1.0627	0.11807	1.2988	0.11807	
Zx*Zy	0.766364	0.136072	2.882452	0.719508	0.578183	0.085437	0.73765	-0.02528	2.21588	0.0314	$\sum Zx*Zy$
											8.127666
											0.9031

$$r = \frac{\sum Zx*Zy}{n-1} = \frac{-8.127666}{9} = 0.9031, \text{ It is a } \underline{\text{STRONG POSITIVE OR DIRECT}} \text{ Relation}$$

- b) (2 mark) What would be the error in the predicted value of the battery life for a tablet that costs 350 UD Dollars?

$$\hat{y} = b_0 + b_1 X$$

$$b_1 = r \frac{S_y}{S_x} = 0.9031 \frac{1.2704}{104.1559} = 0.011, b_0 = \bar{y} - b_1 \bar{x} = 9.35 - (0.011)(422.3) = 4.7407$$

$$\hat{y} = b_0 + b_1 X = \underline{\hat{y} = 4.7407 + 0.011 X}$$

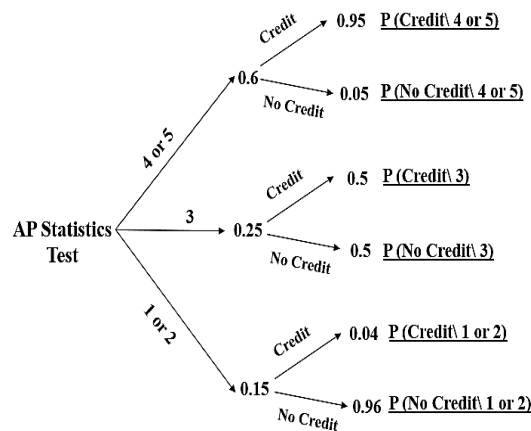
$$\text{At } X = 350 \quad \hat{y} = 4.7407 + 0.011 (350) = \underline{8.5547}$$

$$\text{Error} = |8.5547 - 8| = \underline{0.5547}$$

**Question 3:****marks: 5**

Suppose that 60% of students who take the AP Statistics exam score 4 or 5, 25% score 3, and the rest score 1 or 2. Suppose further that 95% of those scoring 4 or 5 receive college credit, 50% of those scoring 3 receive such credit, and 4% of those scoring 1 or 2 receive credit.

- a) (3 mark) What is the probability that a student will get a college credit?



$$P(\text{Credit}) = P(\text{Credit} \cap 4 \text{ or } 5) + P(\text{Credit} \cap 3) + P(\text{Credit} \cap 1 \text{ or } 2)$$

$$P(\text{Credit}) = P(\text{Credit} \setminus 4 \text{ or } 5) P(4 \text{ or } 5) + P(\text{Credit} \setminus 3) P(3) + P(\text{Credit} \setminus 1 \text{ or } 2) P(1 \text{ or } 2)$$

$$P(\text{Credit}) = (0.95)(0.6) + (0.5)(0.25) + (0.04)(0.15) = \underline{\underline{0.701}}$$

- b) (2 mark) If a student who is chosen at random from among those taking the exam receives college credit, what is the probability that she received a 3 on the exam?

$$P(3 \setminus \text{Credit}) = \frac{P(\text{Credit} \setminus 3) P(3)}{P(\text{Credit})} = \frac{(0.5)(0.25)}{0.701} = \underline{\underline{0.178}}$$

*With My Best Regards,*

*Prof. Dr. Mohamed El-Sharkawy*

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